

Detailing protein solvation shell in an aqueous mixture: a SANS study



WATER INTERFACES
IN PHYSICS,
CHEMISTRY AND
BIOLOGY: A MULTI-
DISCIPLINARY
APPROACH

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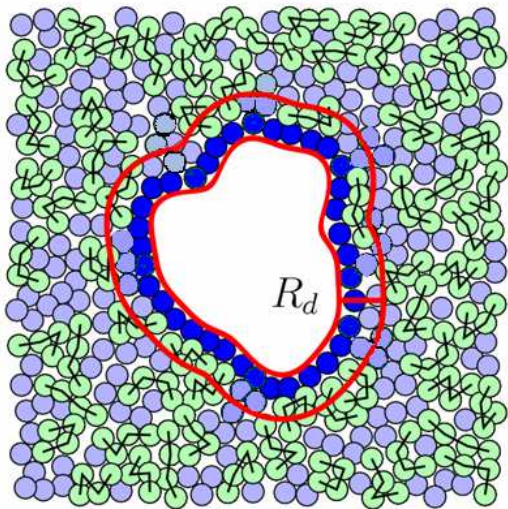
University Polytechnic of Marche,
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Ancona, Italy

Outlook

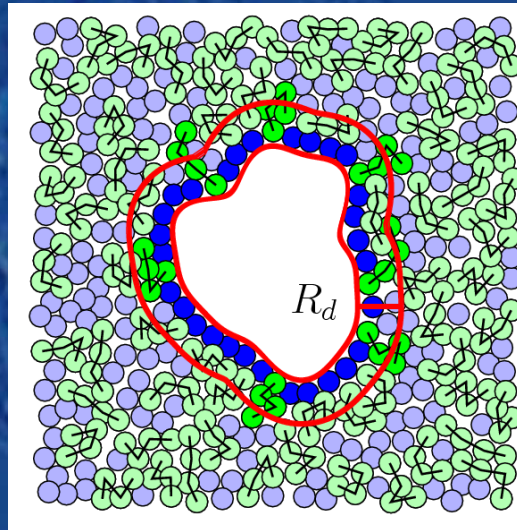
- Small Angle Neutron Scattering
- Protein-solvent interface in water mixtures
- Thermodynamic model for preferential hydration
- SANS data Global fit
- Lysozyme in presence of glycerol and urea:
comparing results

Protein-solvent interface in water mixtures

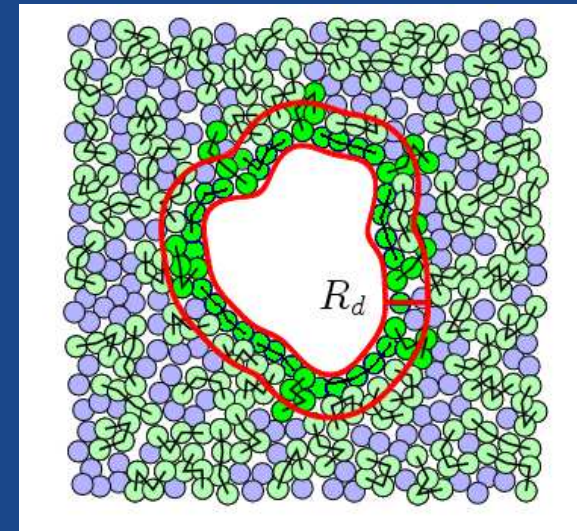
Just water



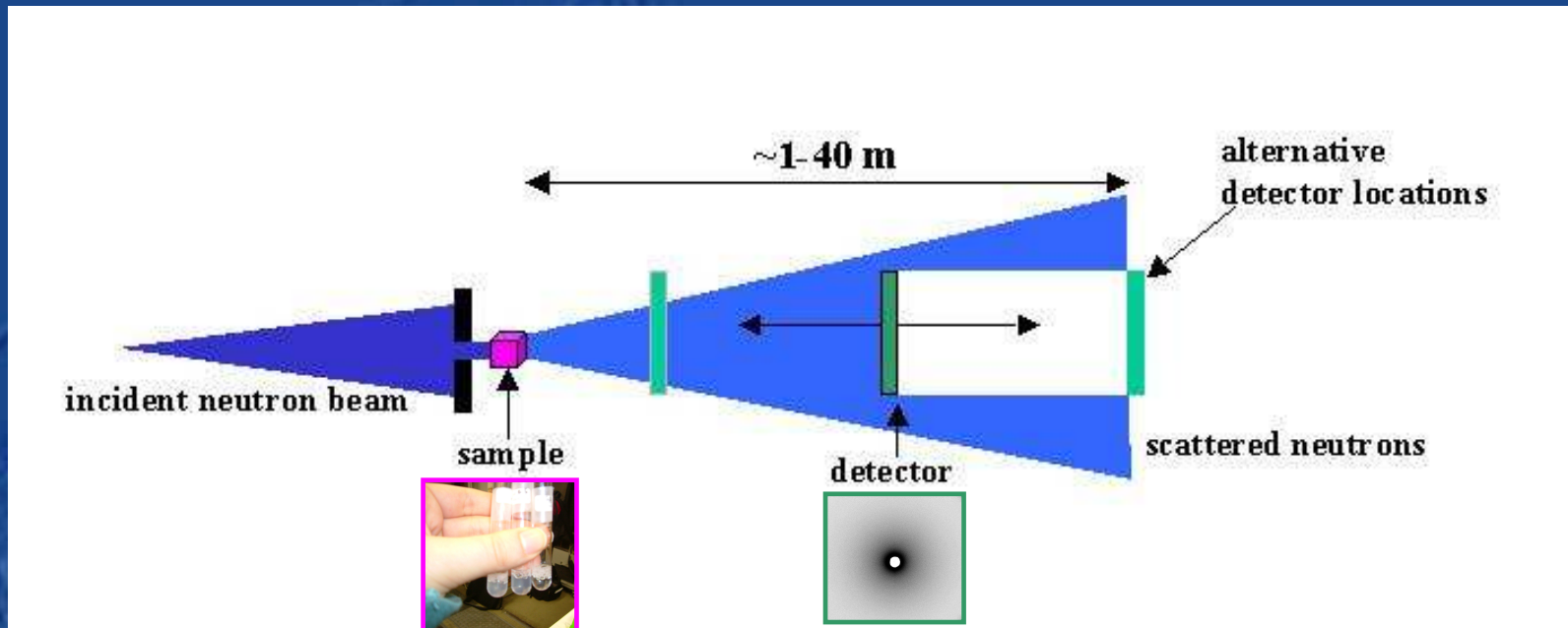
Water & cosolvent



Just cosolvent



Small Angle Neutron Scattering



Despite SANS is a low resolution technique, we have many advantages:

nearly
physiological
conditions

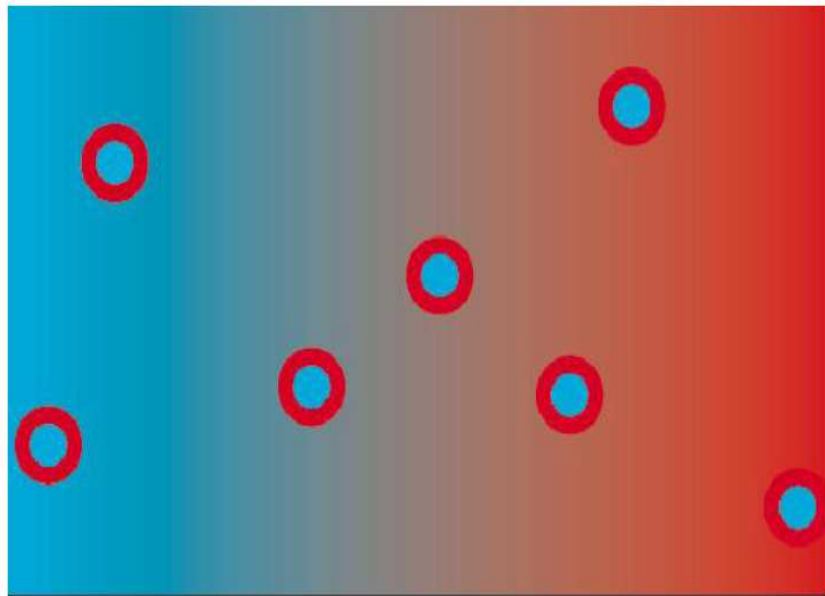
detail the bound water

statistical
“ensemble” over
all particles

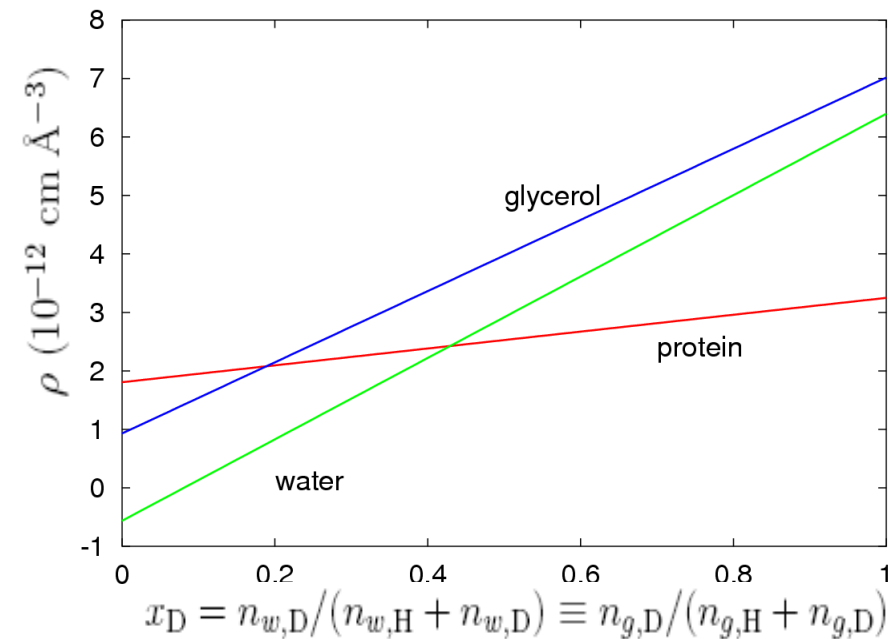
measure interactions

...the major advantage in our case is the contrast variation

$$\Delta\rho = \rho_{\text{protein}} - \rho_{\text{solvent}}$$



Inhomogeneity



富士嶽三十六景 神奈川沖
浪裏

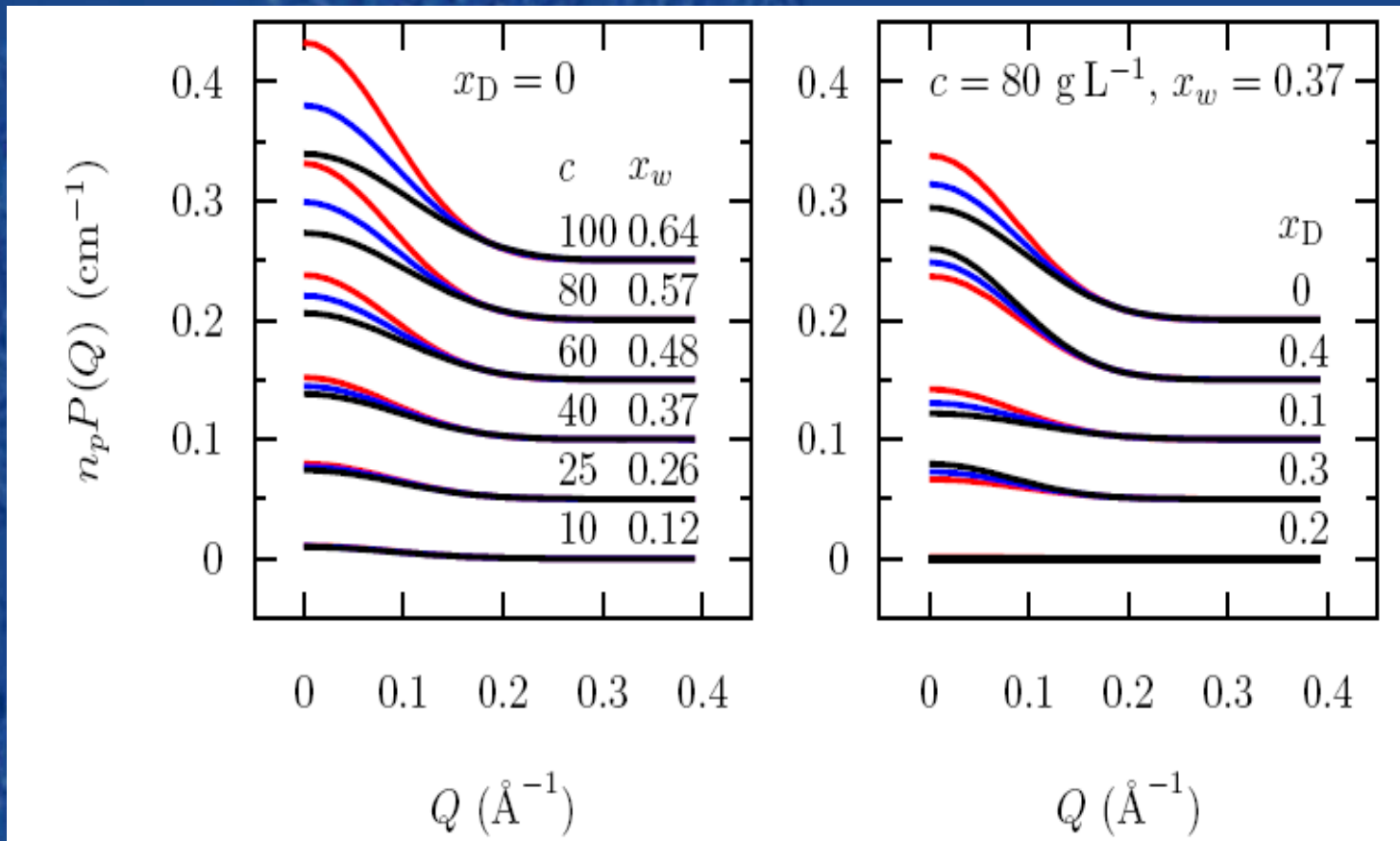
大井 正徳 画



Numerical simulation of SANS curves, calculated in the approximation $S_M(Q)=1$.

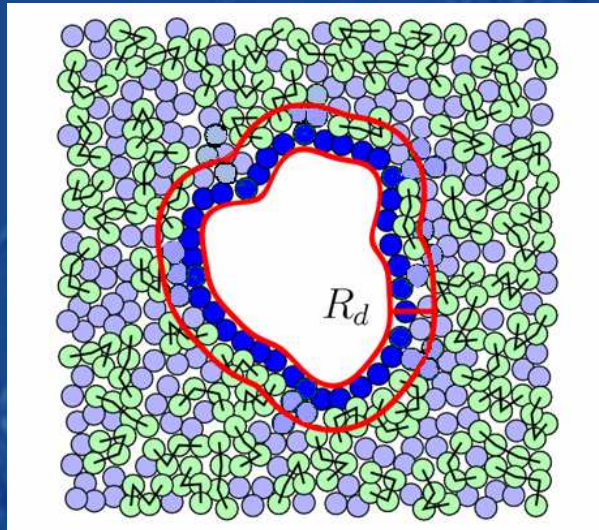
$$\frac{d\Sigma}{d\Omega}(Q) = n_p P(Q) S_M(Q)$$

$$\frac{x_{w,l}}{x_w} = 1, 1.2, 1.4$$

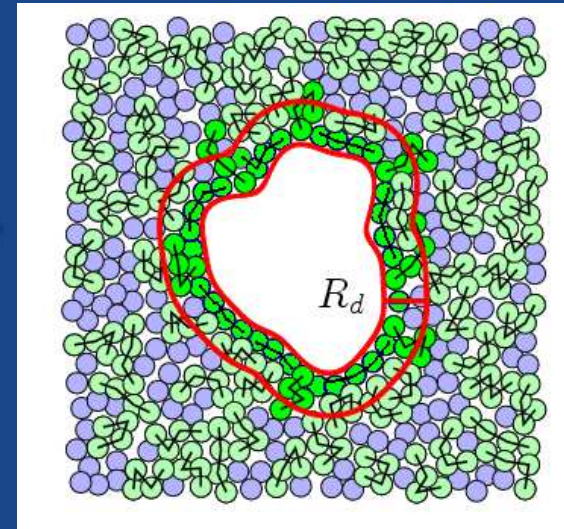


Protein-solvent interface in water mixtures

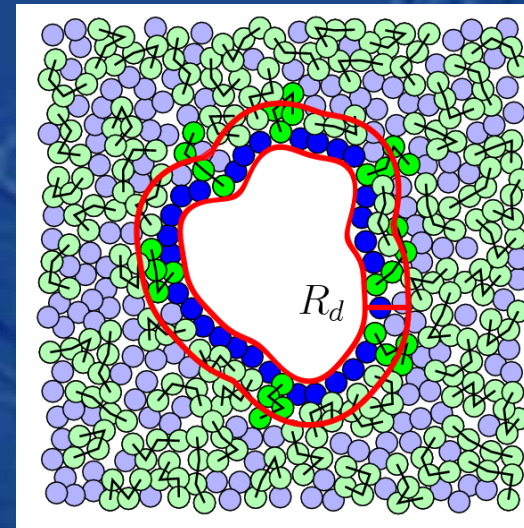
Just water



Just cosolvent



Thermodynamic equilibrium



Scaled representations of a solvated lysozyme molecule based on PDB structure (6LYZ).

○, ● water molecules in the bulk and in the first solvation layer.

○, ● glycerol molecules in the bulk in contact with the protein.

Thermodynamic model* for preferential hydration

$$c_l + w_b \square c_b + w_l$$

c: cosolvent
w: water
l: local domain
b: bulk

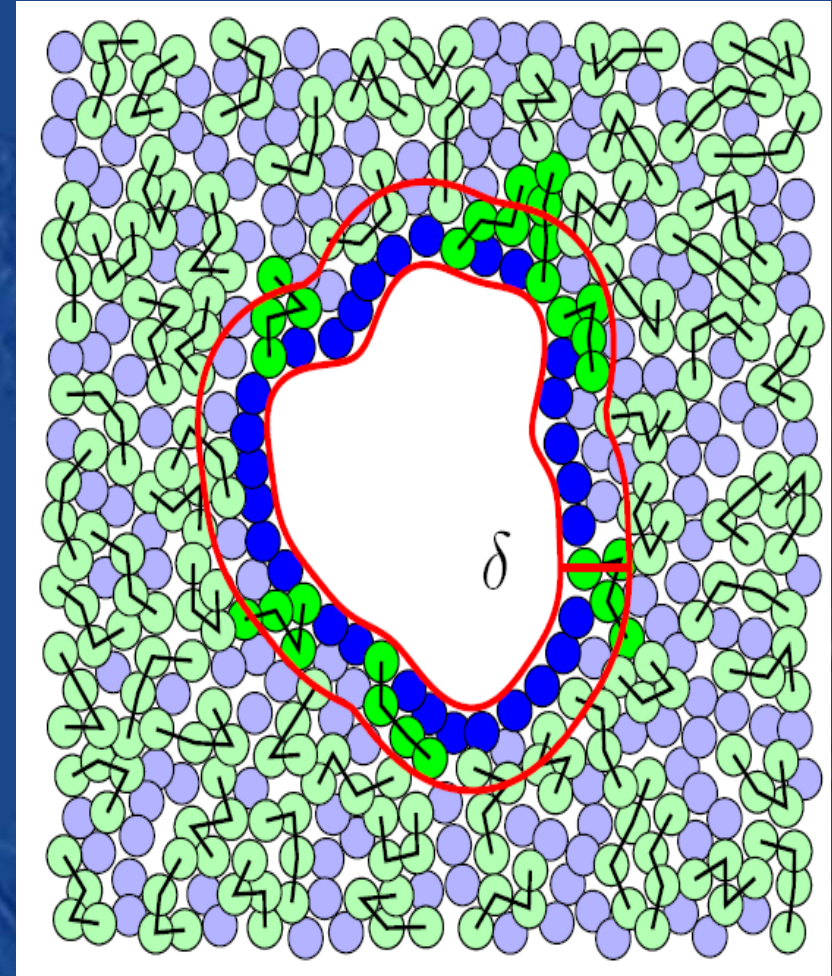
$$K = \frac{x_{w,l}}{1 - x_{w,l}} \frac{1 - x_{w,b}}{x_{w,b}}$$

$x_{w,i}$ water molar fraction in the *i*-th domain

$$x_{w,l} = \frac{n_{w,l}}{n_p m}$$

m: number of sites

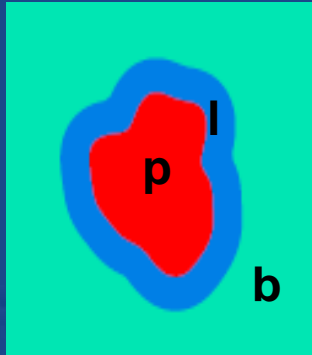
if $K > 1$ preferential interaction with water
 if $K < 1$ preferential interaction with cosolvent



* J. A. Schellmann, Biophys. J. 85, 108 (2003).

SANS data Global fit

Three phase Form Factor



$$P(Q) = (\rho_p - \rho_b)^2 V_p^2 P_{pp}(Q) + (\rho_l - \rho_b)^2 V_l^2 P_{ll}(Q) + 2(\rho_p - \rho_b)(\rho_l - \rho_b) V_p V_l P_{pl}(Q) +$$

$V_{w,i}, V_{c,i}$

partial molecular volumes of water and cosolvent in the i -th domain

a_w, a_c

scattering lengths of water and cosolvent at x_D

$$\rho_i = \frac{x_{w,i}(a_w - a_c) + a_c}{x_{w,i}(V_{w,i} - V_{c,i}) + V_{c,i}} \quad i=b,l$$

$$K = \frac{x_{w,l}}{1 - x_{w,l}} \frac{1 - x_{w,b}}{x_{w,b}}$$

Effective Structure Factor

Under the Random Phase Approximation (RPA)

$$u_C(r) = \frac{Z^2 e^2}{\epsilon (1 + \kappa_D R)^2} \frac{\exp[-\kappa_D(r - 2R)]}{r}$$

$$u_A(r) = -2JR \frac{\exp[-(r - 2R)/d]}{r}$$

Effective Structure Factor

Under the Random Phase Approximation (RPA)

$$S_M(Q) = \frac{S_0(Q)}{1 + \beta n_p S_0(Q) [U_C(Q) + U_A(Q)]}$$
$$[S_0(Q)]^{-1} = 1 - \frac{12\eta[\eta(3 - \eta^2) - 2] j_1(2RQ)}{(1 - \eta)^4 2RQ}$$

$S_0(Q)$ structure factor relative to the hard sphere potential

$\beta = 1/k_B T$

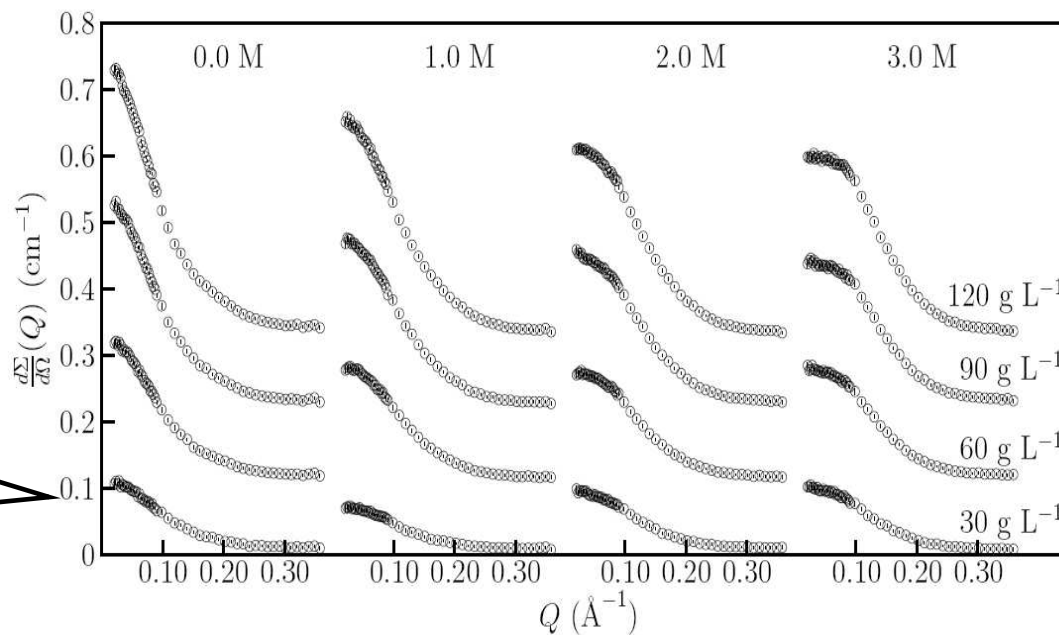
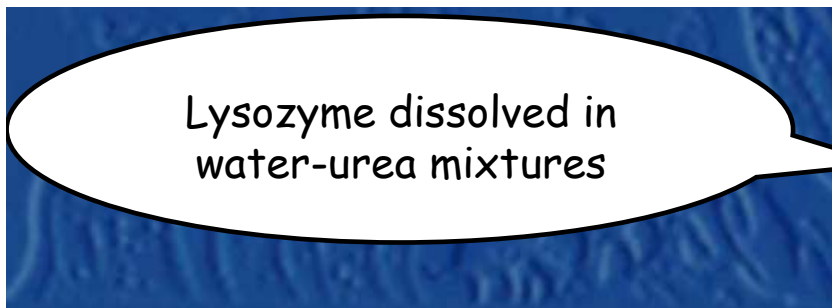
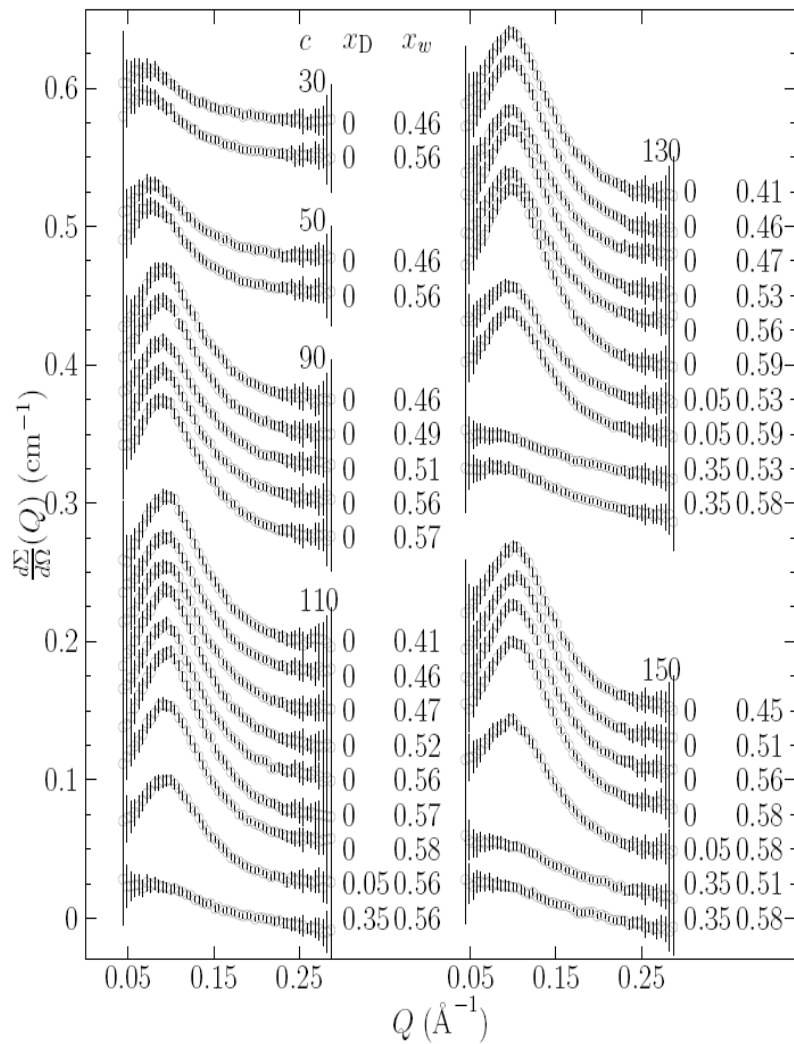
U_C Fourier transform of the screened Coulombic potential

U_A Fourier transform of the attractive potential

η protein volume fraction

$$u_C(r) = \frac{Z^2 e^2}{\epsilon (1 + \kappa_D R)^2} \frac{\exp[-\kappa_D (r - 2R)]}{r}$$

$$u_A(r) = -2JR \frac{\exp[-(r - 2R)/d]}{r}$$



SANS data Global fit

Fixed
parameters

$$v_{w,b}$$

$$v_{c,b}=v_{c,1}$$

Fitting
parameters

K

Z

v_p

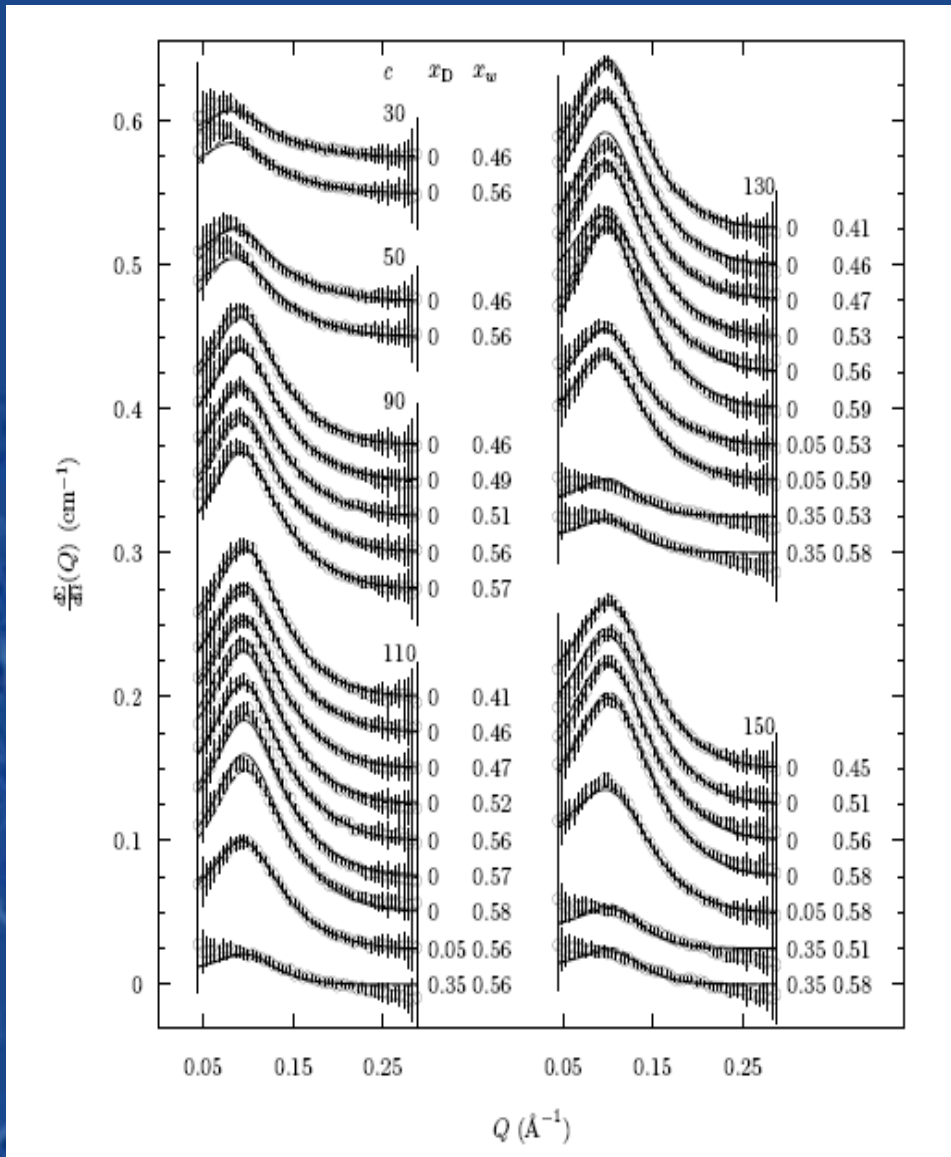
J

d

δ_1

$v_{w,1}$

Lysozyme dissolved in water-glycerol mixtures*

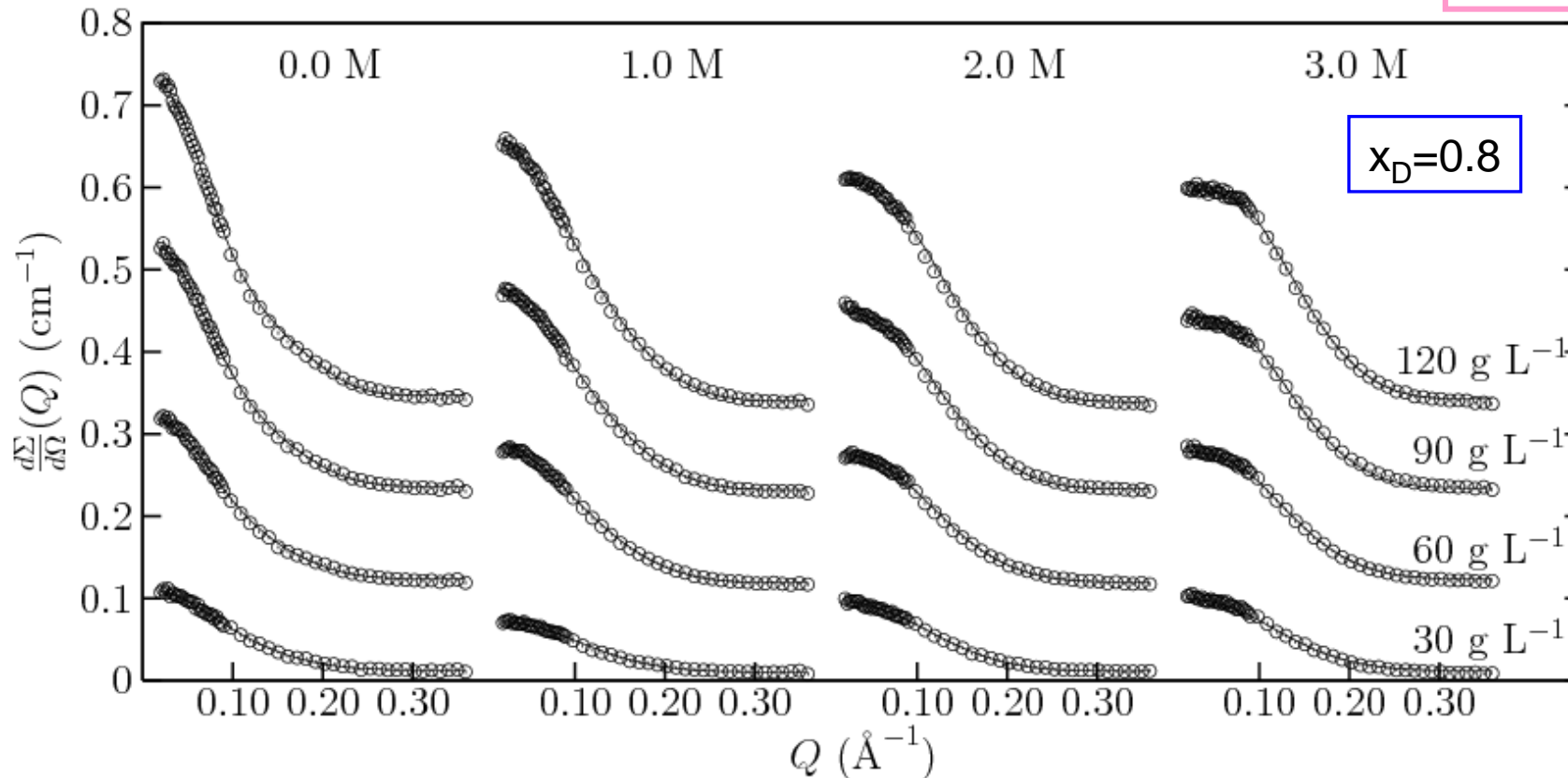
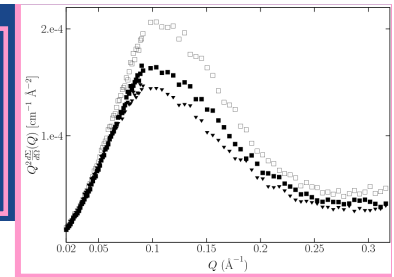


Experimental scattering curves collected at the nuclear reactor of Forschungszentrum Jülich on 35 different samples. Solid lines correspond to the global fit with K common to all experimental curves.

*R. Sinibaldi, M.G. Ortore, F. Spinozzi, F. Carsughi, H. Frielinghaus, S. Cinelli, G. Onori and P. Mariani. "Preferential hydration of lysozyme in water/glycerol mixtures: a small-angle neutron scattering study". *Journal of Chemical Physics*, 126, 235101 (2007).

Lysozyme in presence of urea*

Kratky plots for lysozyme solution (60 mg/ml) with urea from 1 to 3 M

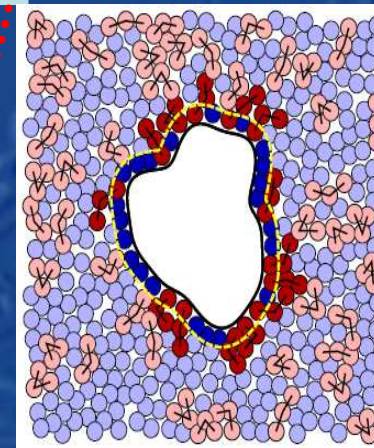
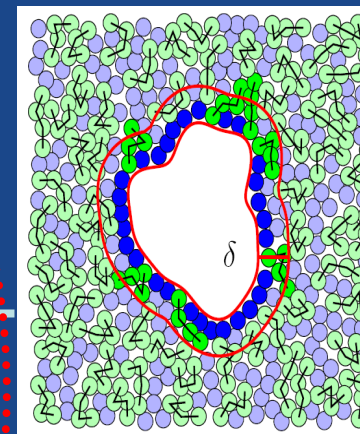


Experimental scattering curves collected at the nuclear reactor of Hahn Meitner Institut in Berlin on 16 different samples. Solid lines correspond to the global fit with K common to all experimental curves.

*M.G. Ortore, R. Sinibaldi F. Spinuzzi, F. Carsughi, D. Clemens, A. Bonincontro and P. Mariani. "New insights into urea action on proteins: SANS and Zeta Potential study of lysozyme". Submitted to *J. Phys. Chem. B*

Comparing results

	$V_p (\text{\AA}^3)$	$\delta_1 (\text{\AA})^*$	$v_{w,1} (\text{\AA}^3)^\#$	$Z (e)$	K
Lysozyme with glycerol	17060 ± 70	5.9 ± 0.2	28.81 ± 0.04	9.00 ± 0.04	1.87 ± 0.03
Lysozyme with urea	16950 ± 100	3.8 ± 0.6	27.5 ± 0.5	$2.0 \rightarrow 8.0$	0.52 ± 0.08

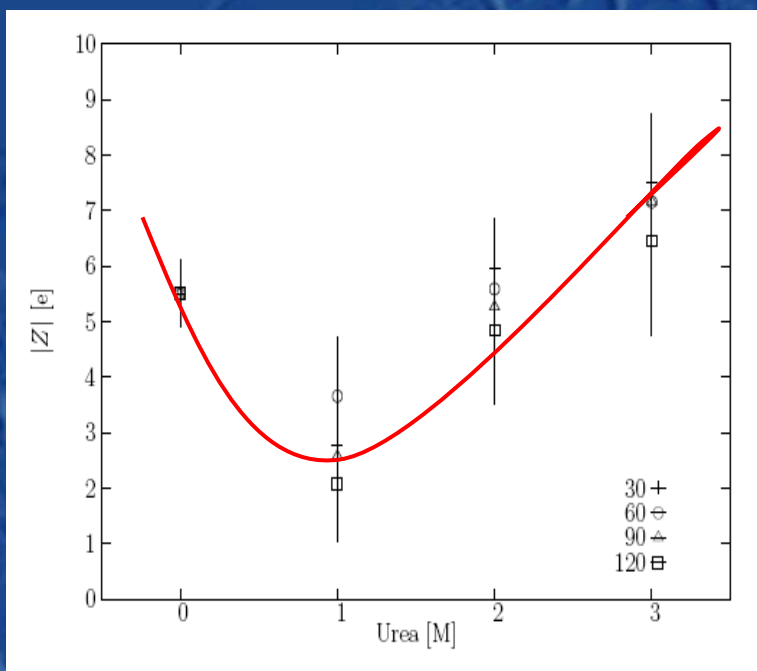


*B. M. Baynes and B. L. Trout, J. Phys. Chem. B **107**, 14058 2003

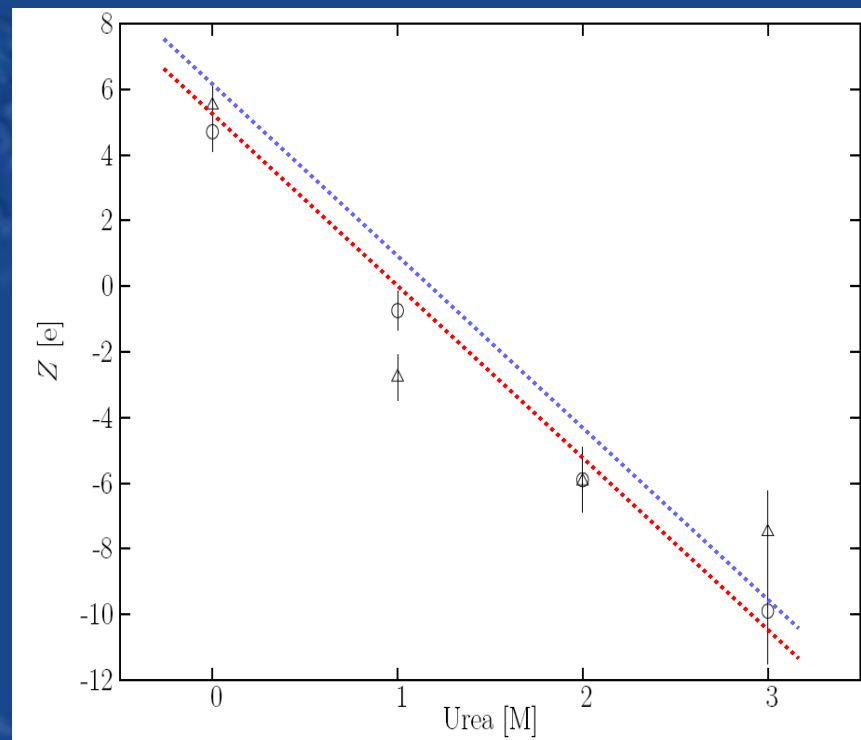
#D. I. Svergun, S. Richards, M. H. J. Koch, Z. Sayers, S. Kuprin and G. Zaccai
Proc. Natl. Acad. Sci. USA Vol. 95, pp. 2267–2272, 1998

Lysozyme effective charge in urea-water mixtures

SANS Global fitting results



Zeta-potential measurements

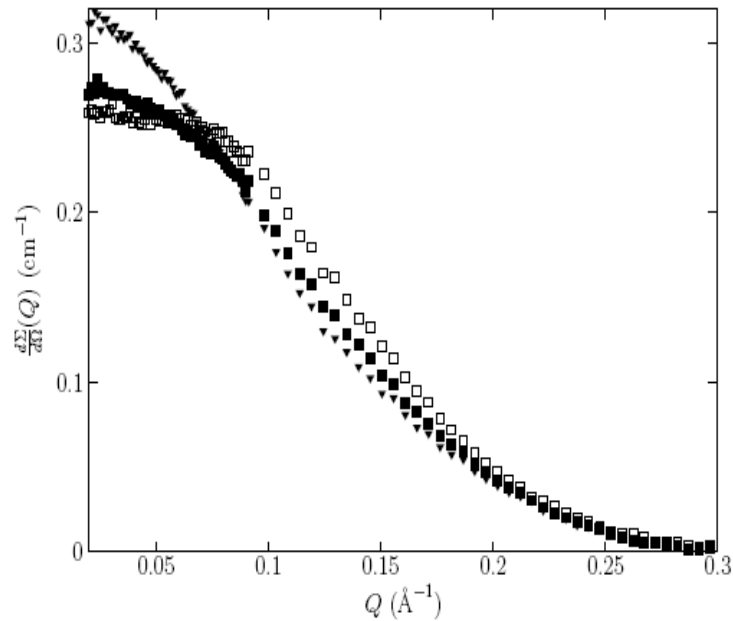


Surface charge density

$$\sigma = \frac{\epsilon \zeta}{4\pi\tau}$$

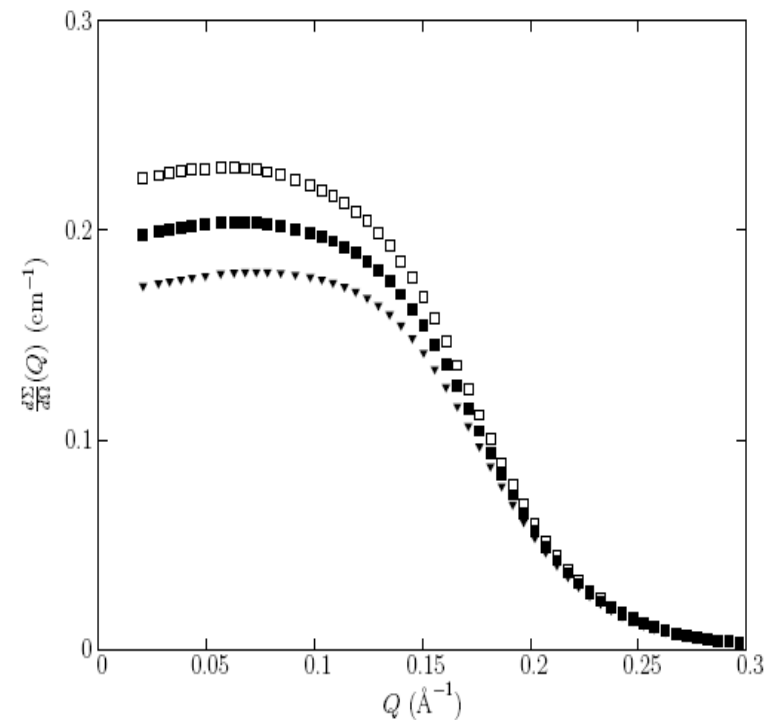
ζ : measured Zeta-potential

τ : thickness of the electric double layer



SANS experimental differential cross sections at $c=120\text{gL}^{-1}$ and different amounts of urea in solution. Symbols refer to different urea concentrations: triangles 1 M, full squares 2 M and empty squares 3 M.

Numerical simulated differential cross sections regarding the same experimental conditions. The scattering length densities of bulk solvent and local domain have been calculated considering the local domain enriched by a 10% of urea with respect to the nominal bulk composition, and assuming a constant protein charge $Z = 6$ in the coulombic potential and a constant attractive term ($J = 3k\text{BT}$ and $d = 3\text{\AA}$). Only the dielectric constant was considered to vary with urea concentrations from 78.3 to 82.5 as a function of the urea solvent concentration.



Lysozyme-glycerol

J and d parameters, which describe the attractive potential, are smoothly dependent on solvent composition, confirming that glycerol can prevent protein-protein aggregation,

x_w	J ($k_B T$)	d (\AA)
	$I_S = 32 \pm 4$ mM	
0.46	2.36 ± 0.09	5.2 ± 0.2
0.56	3.74 ± 0.09	2.7 ± 0.2

Lysozyme-urea

we considered the depth J to linearly vary with water molar fraction in solution and to be independent on protein concentration: $J = J_0 + J_m x_w$.

J decreases adding urea in solution

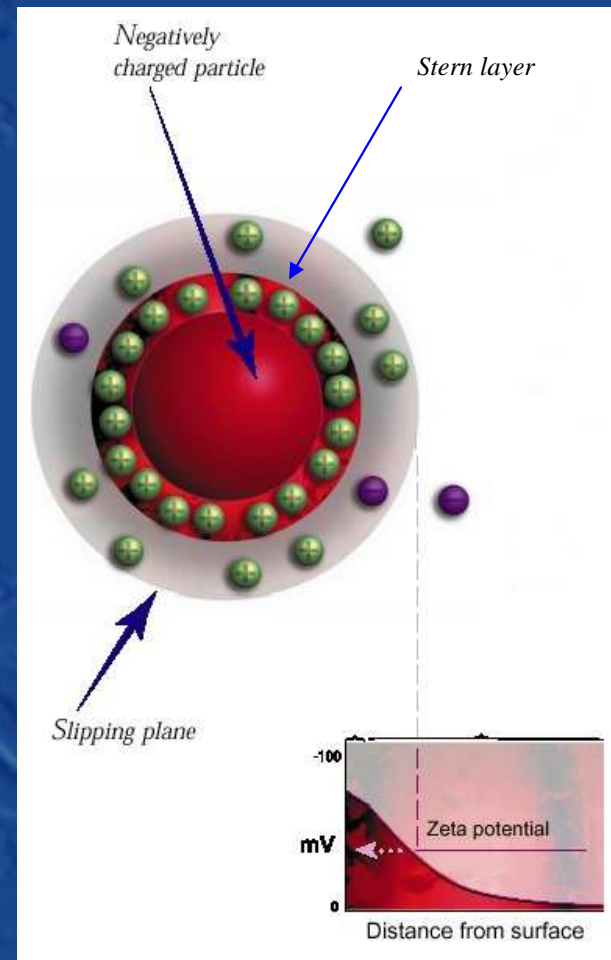
J_0 ($k_B T$)	J_m ($k_B T$)	d (\AA)
-7.7 ± 0.3	12 ± 2	2.5 ± 0.5

Lysozyme effective charge in urea-water mixture

Zeta-potential measurements

- an electrical double layer exists around charge particles in solution;
- the liquid layer surrounding the particle exists as two parts; an inner region (Stern layer) where the ions are strongly bound and an outer (diffuse) region where they are less firmly associated;
- within this diffuse layer is a *notional* boundary known as the slipping plane, within which the particle acts as a single entity;
- the potential at this boundary is known as **Zeta Potential**, which depends on the protein net charge.

T=13 Angstrom, surface:6500 Angstrom²



Comparison with literature

The preferential binding coefficient

$$\Gamma_{pj} = \lim_{n_p \rightarrow 0} \left(\frac{\partial n_j}{\partial n_p} \right)_{P,T,\mu_j} \quad j=w,c$$

$$\Gamma_{pj} = n_j (G_{pj} - G_{wc})$$

Kirkwood-Buff integrals

$$G_{ij} = \int_{-\infty}^{+\infty} dr [g_{ij}(r) - 1]$$

Radial distribution function

Calculated in the limit $n_p \rightarrow 0$

$$\Gamma_{pj} = mx_{j,l} + \frac{x_j}{v_{w,b}x_w + v_c x_c} \left[\frac{v_{w,b}v_c}{v_{w,b}x_w + v_c x_c} - V_p - m(v_{w,l}x_{w,l} + v_c x_{c,l}) - k_B T k_T \right]$$

The excess solvation number

$$N_{pj} = n_j G_{pj}$$

Number of displaced molecules j when a protein molecule is introduced into the mixed solvent

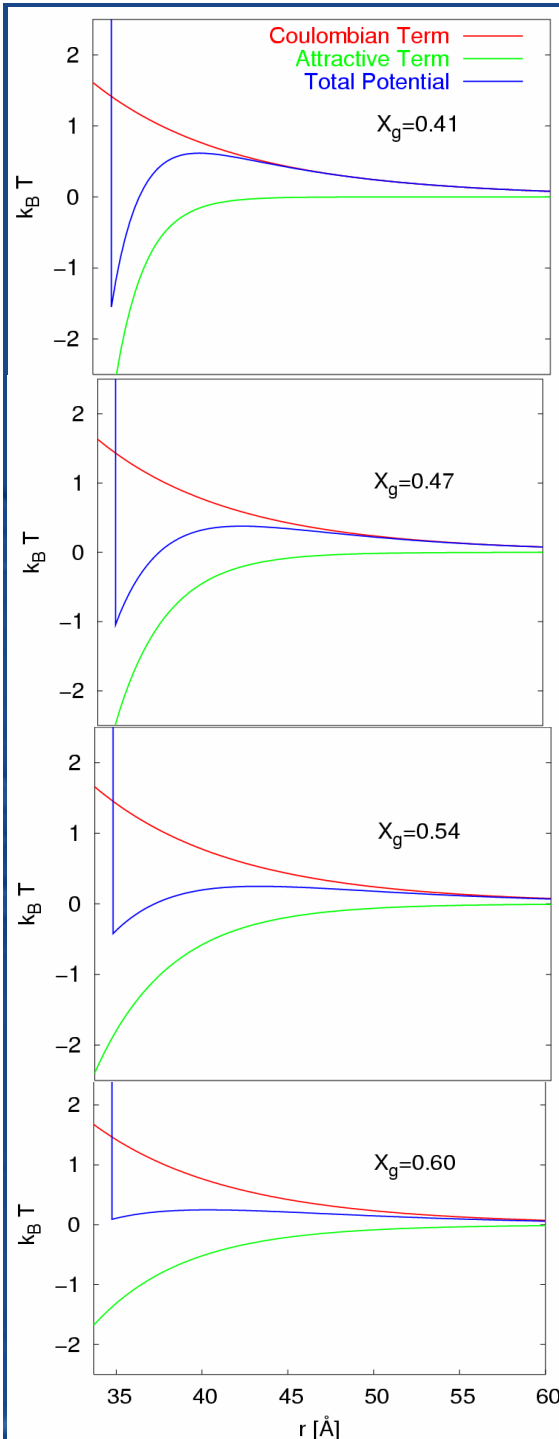
Protein-Protein interaction varies with the glycerol molar fraction

The structure factor $S_M(Q)$ contains information about the protein-protein correlation. It has been modeled using a three component integrable pair potential including Hard Sphere, Attractive term and Coulombian Term*.

$$u(r) = u_{HS}(r) + u_C(r) + u_A(r)$$

$$u_A(r) = -J\sigma \frac{\exp[-(r - \sigma)/d]}{r}$$

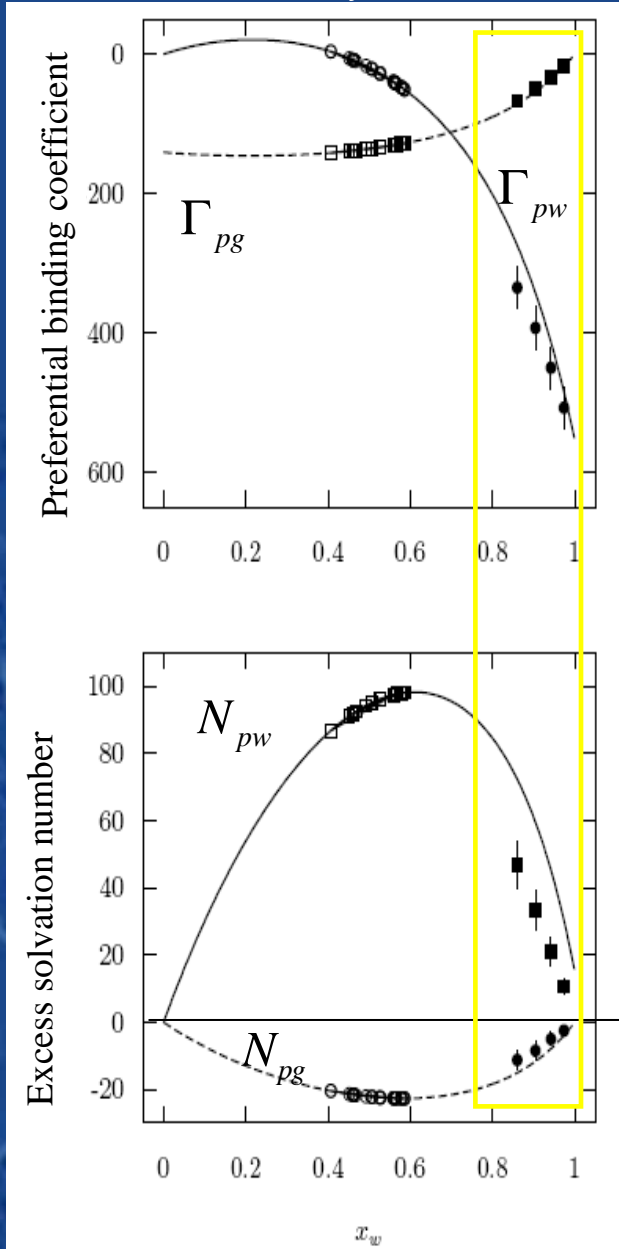
J and d are fit parameter that depend on the water molar fraction in solution. σ is the protein diameter and correspond to the Hard sphere parameter.



*J.Narayanan X.Y.Liu Biophys. J. 84, 523 (2003).

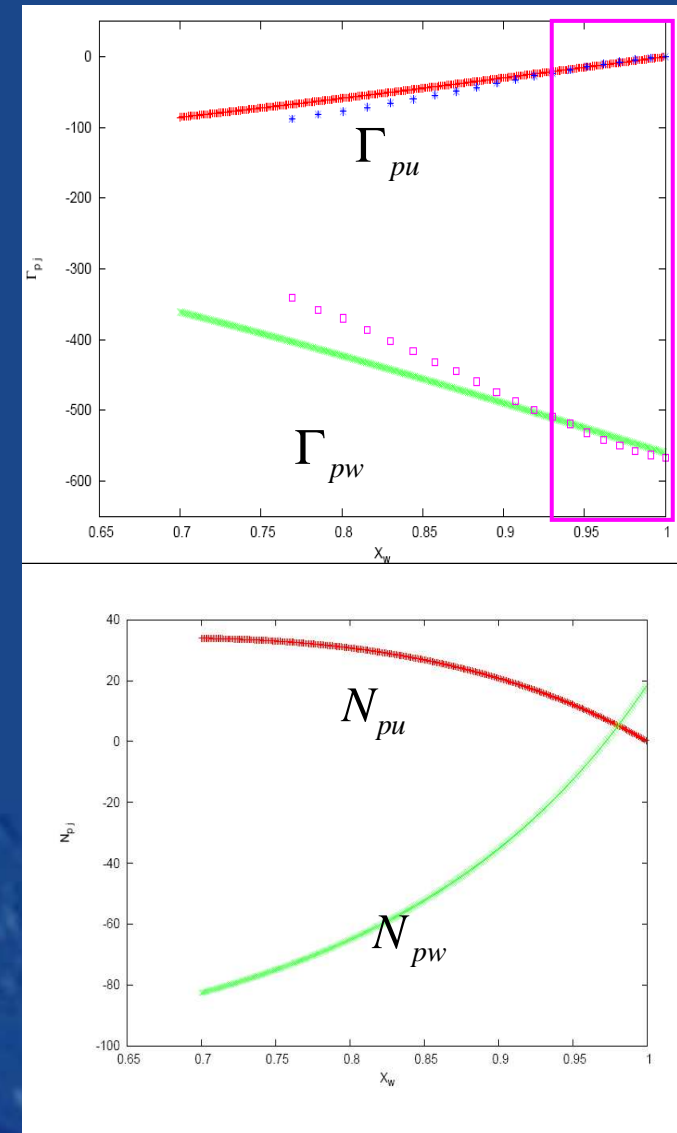
Glycerol in the solvent enhances the amount of water in the solvation layer*.

Urea accumulates in excess around the peptide, confirming MD and Timasheff literature results #.



The preferential binding coefficient

$$\Gamma_{pj} = \lim_{n_p \rightarrow 0} \left(\frac{\partial n_j}{\partial n_p} \right)_{P,T,\mu_j} \quad j=w,c$$



*G. Kekko and S.M. Timasheff *Biochemistry* 1981, 20: 4667-4676

S. N. Timasheff and G. Xie *Biophys. Chem.* 2003; 105, 421-448

Concluding remarks

- In-solution SANS technique associated to global fit analysis can *quantitatively* detail the properties of protein solvation shell
- Confim of MD results: thickness of the local domain
- Confim of previous SAXS/SANS results: densier water in the solvation shell
- Perspectives in protein-protein interactions in organic mixtures

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